

Time : 2 Hrs.

Marks : 60

Note : 1] Section I is compulsory .

2] Attempt any three questions out of four questions from section II.

3] Simple calculators are allowed.

**Section - I**

Q.1 Attempt any Three of the following. 15

a) If  $A = \begin{bmatrix} 4 & 2 \\ -3 & 1 \end{bmatrix}$  ,  $B = \begin{bmatrix} 5 & 1 \\ 3 & -1 \end{bmatrix}$

Prove  $(AB)^T = B^T A^T$

b) If  $A = \begin{bmatrix} 2 & 3 \\ 7 & 5 \end{bmatrix}$  ,  $B = \begin{bmatrix} 0 & -1 \\ -3 & 0 \end{bmatrix}$  ,  $C = \begin{bmatrix} 3 & -3 & 8 \\ 4 & -2 & 7 \end{bmatrix}$

Prove that  $A(BC) = (AB)C$ .

c) Find  $\frac{dy}{dx}$  if (i)  $y = (x^3 - \sqrt{x} + \log x) (3e^x + 5^x)$   
 (ii)  $y = (5x^3 + 6x^2 + 2) (2^x - \log x)$

d) The sequence of 3 numbers a, b, c is an A.P. whose sum is 18. If a & b are each increased by 4 & C is increased by 36, the new numbers form a G.P. find a, b, c.

Q.2 Attempt any Three of the following 15

a) Given the following transaction matrix, find the input - output coefficient matrix & also write the balance equation.

Purchasing Sector			
Producing	Agriculture	Industry	Final Demand
Agriculture	300	600	100
Industry	400	1200	400

b) Given below the transaction table, find the input - output coefficient matrix & also write the balance equation. (

Purchasing Sector	Industry	Agriculture	Current Demand	Total Output
Producing sector				
Industry	30	40	60	130
Agriculture	20	10	40	70

c) i) Define the Profit Function

ii) The demand function  $P = 1400 - 6x$  & the cost function  $C = 1500 + 80x$ , where x is the output. Find x for which the profit is increasing.

d) Examine the following function for maximum & minimum. Also find maximum & minimum values  $f(x) = x^3 - 24x^2 + 189x + 10$ .

**Section - II**

- Q.3 a) (I) Determine the principal that will earn Rs. 4000 as simple interest in 8 years at 5% p.a. 02**
- (ii) Find the compound interest of Rs.8,000 at the rate of 6% for 1.5 years, if the interest is calculated half yearly. 03**
- Q.3 b) (i) Define EMI. 02**
- (ii) A person borrows Rs.1,00,000 from a bank for a period of 4 years at 9% flat rate of interest. Compute EMI 03**
- Q.4 a) Define : (i) Total Revenue function 06**
- (ii) The Profit function**
- (iii) Total cost function.**
- b) Evaluate : (i)  $\frac{(1-x)^3}{x} dx$  04**
- (ii)  $\frac{(x+1)(x-4)}{\sqrt{x}} dx$  04**
- Q.5 a) (i) What is the present value of an annuity of Rs. 3000 paid at the end of each year for 4 years at 10% p.a.? 06**
- (ii) How many four digit number can be formed using six digits 1, 3, 5, 7, 8 & 9 if (1) No digit is repeated in the same number.**
- (2) repetition of digits is allowed.**
- b) Evaluate :  $\int_1^2 \frac{(1+x^2)}{x} dx$  04**
- Q.6 a) If  $A = \begin{bmatrix} 2 & -3 \\ 4 & -1 \end{bmatrix}$ ,  $B = \begin{bmatrix} -2 & 0 \\ 0 & -2 \end{bmatrix}$  04**
- Find the matrix X s.t AX = B.**
- b) (1) Define Producer Surplus & Consumer Surplus. 06**
- (2) Find the Producer surplus for supply function**
- $P^2 - x = 9$  when  $x_0 = 7$ .**

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